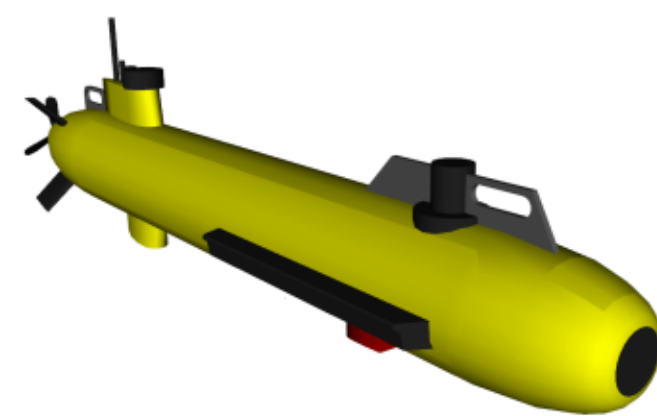


Problem Statement

We study the problem of an Autonomous Underwater Vehicle (AUV) exploring an unknown environment. The AUV has proprioceptive (IMU, DVL ...) and exteroceptive (sonar, cameras ...) sensors embedded.

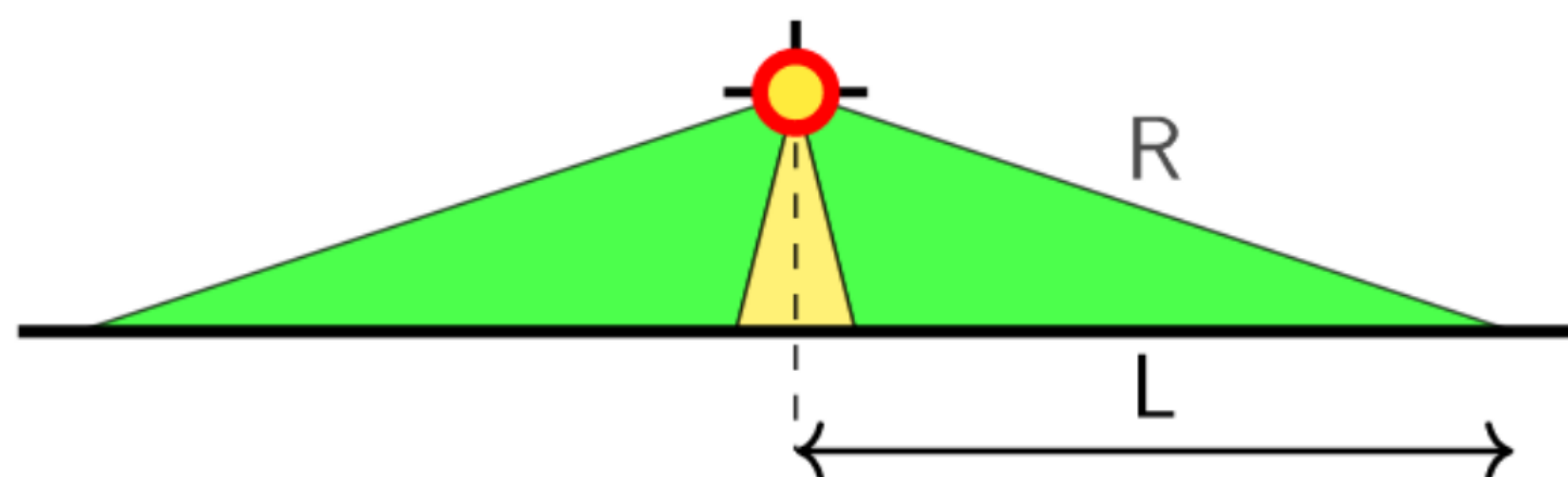
Objectives

Using only the robot's proprioceptive information we would like to compute in real time the explored area and how many times a point in the explored space has been seen by the AUV's exploration sensors.

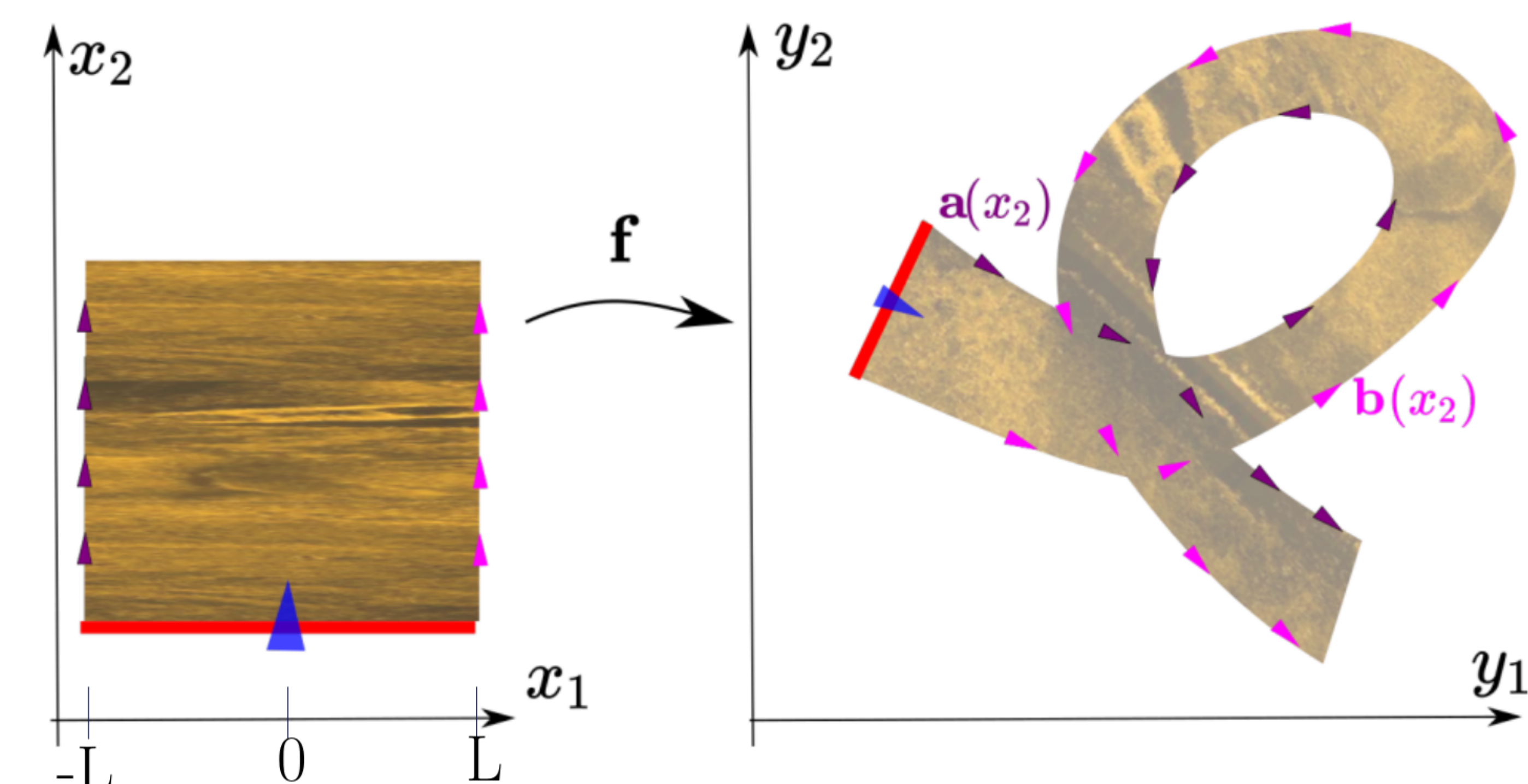
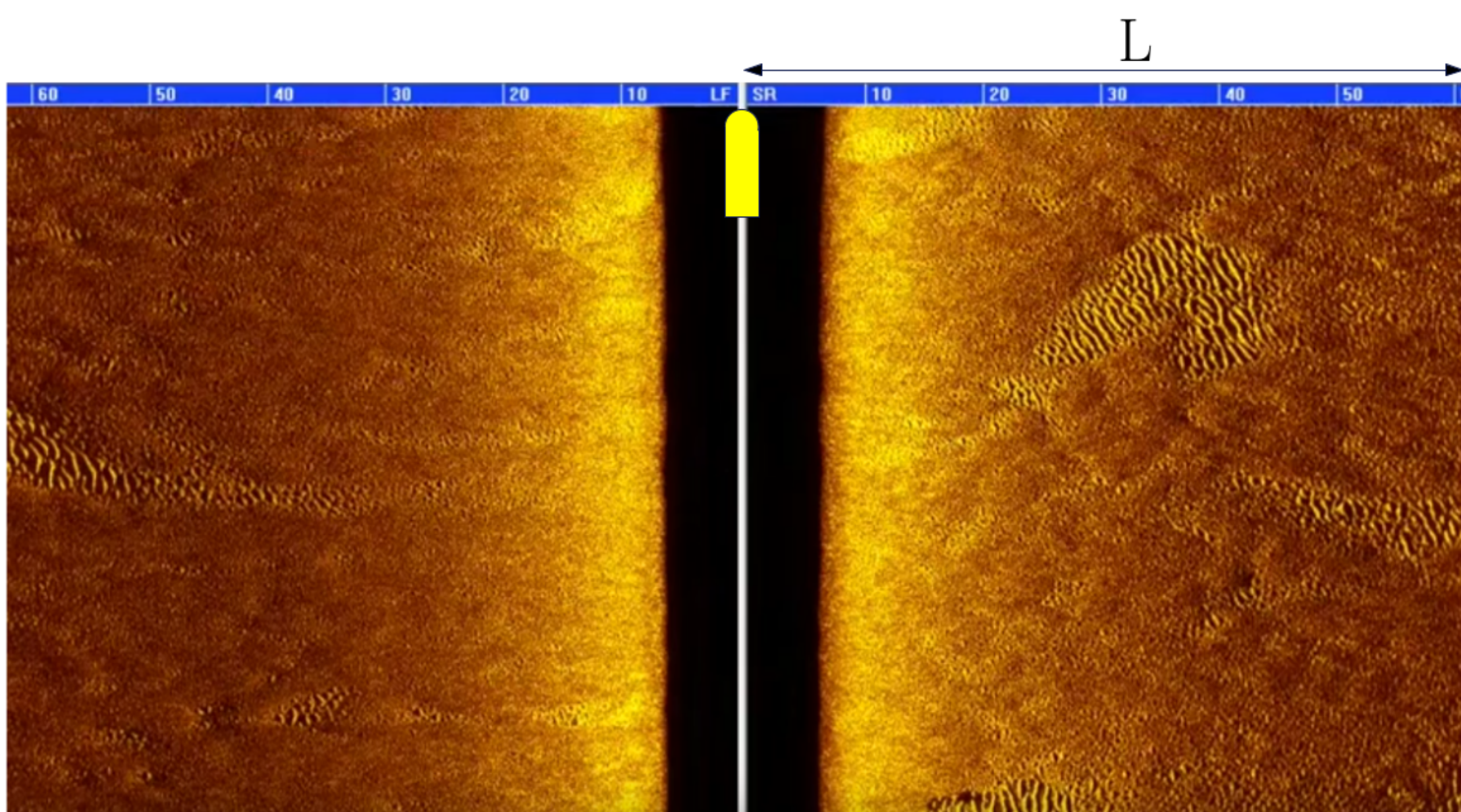


Context

We consider that the AUV has at each side a side scan sonar with a gap filler. At a first moment, for the sake of simplicity, we assume that the dynamics of the system are known and that the proprioceptive sensors are precise.

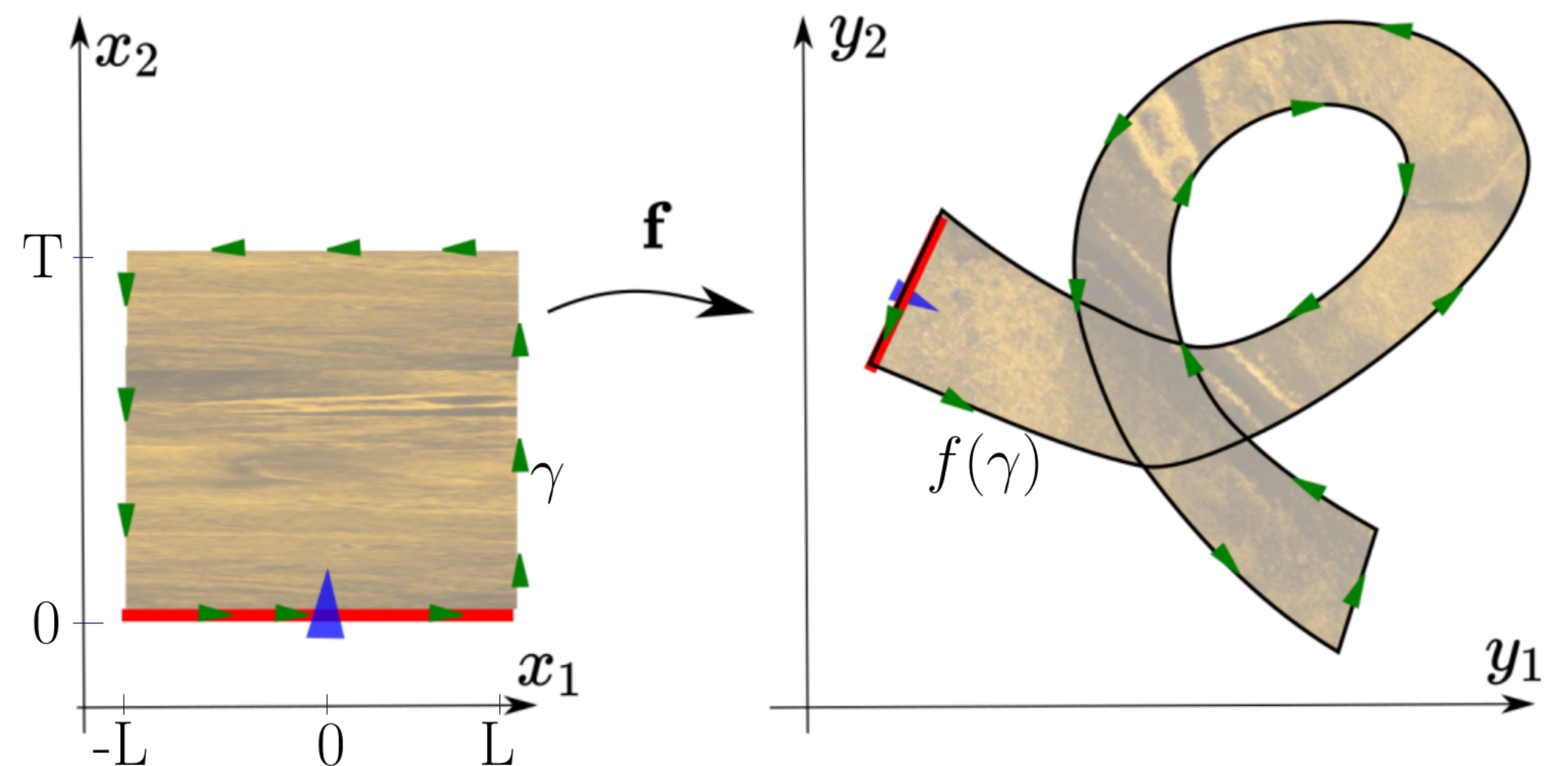


Side scan waterfall :



Contour

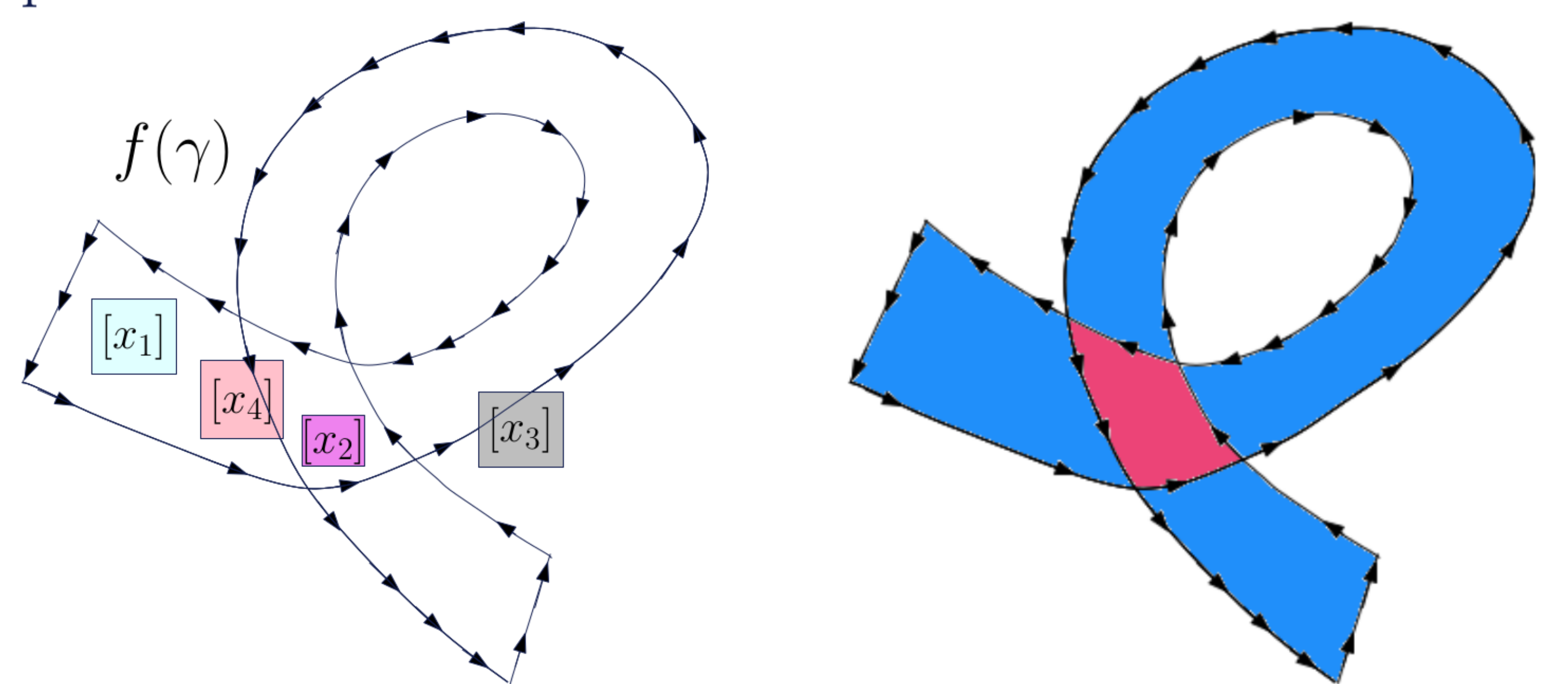
$$f(x_1, x_2) = a(x_2) \cdot \frac{(1 - \frac{x_1}{L})}{2} + b(x_2) \cdot \frac{(1 + \frac{x_1}{L})}{2}$$



The question "How many times has a point been seen by the robot ? " is equivalent to "How many times has a point been surrounded by the contour $f(\gamma)$?"

Winding Number

Winding numbers are an important concept in algebraic topology. The winding number of a closed curve with respect to a point is an integer that represents the total number of times the curve surrounds the point in a counterclockwise manner. A negative winding number counts clockwise turns around the point.



Conclusions

Using the properties of winding numbers and interval analysis we were able to compute in less than a second the area explored by an AUV in a simulated environment of $1250m^2$.

Future Work

- Add uncertainty to the robot's estimated trajectory
- Test the algorithm in real time in a real environment