

# Resource Allocation and Optimization for the Non-Orthogonal Multiple Access

IDIA students'day, Institut Polytechnique de Paris

PhD student: Lou Salaün

Supervisors: Prof. Marceau Coupechoux, Télécom Paris, France  
Dr. Chung Shue Chen, Nokia Bell Labs, Paris-Saclay, France

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# Context

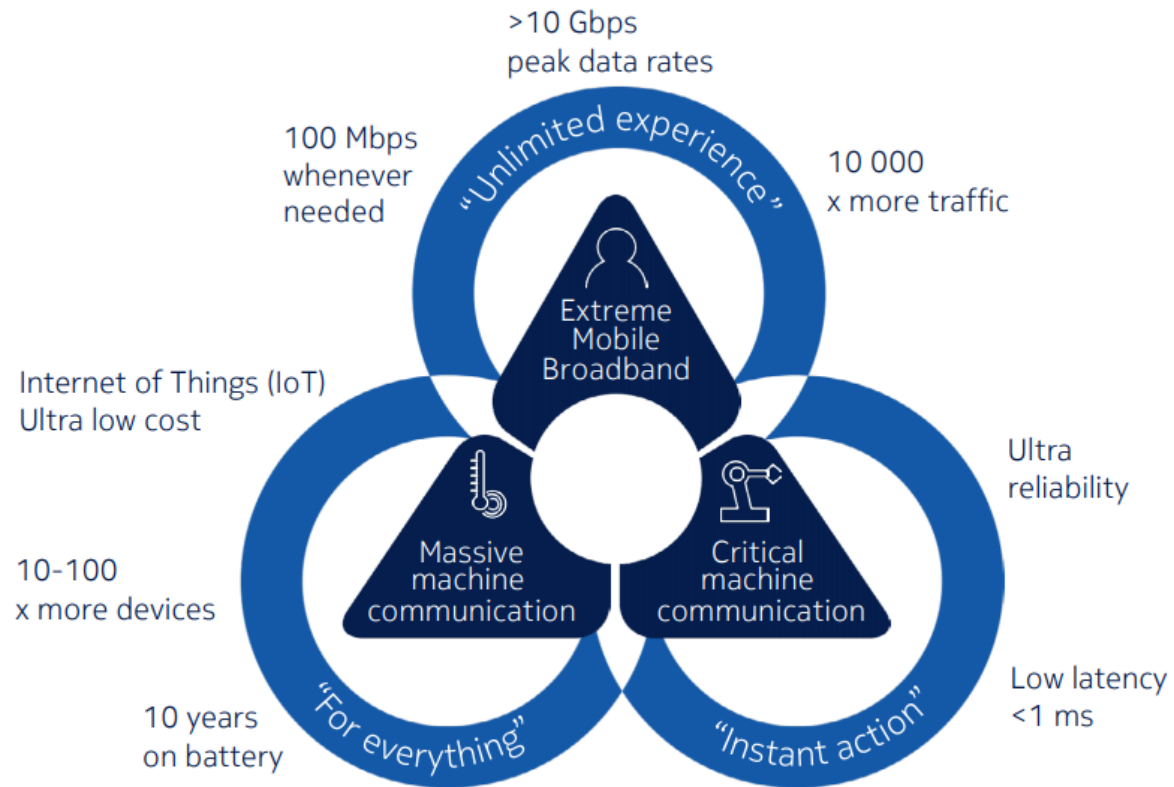


Fig. 5G enables new capabilities beyond mobile broadband

[White paper: 5G new radio network, use cases, spectrum, technologies and architecture," Nokia, Tech. Rep., 2019]

# Non-Orthogonal Multiple Access (NOMA)

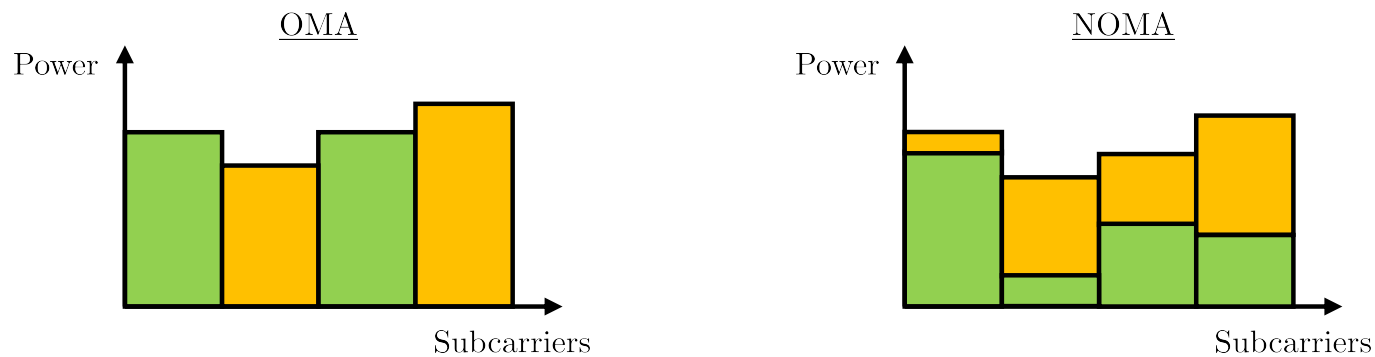
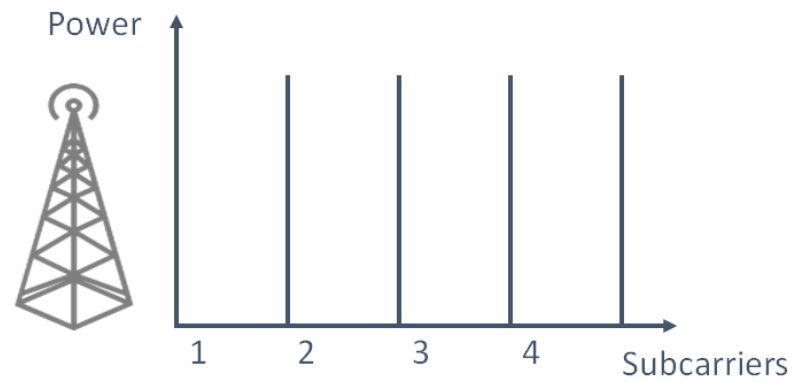


Fig. OMA vs NOMA. The two colors represent the transmit power of two different users' signals

- NOMA allows to superpose several signals on the same subcarrier in the power domain:
  - Increase network spectral efficiency
  - Support massive connectivity
  - Improve cell-edge users performance
  - Complex decoding (interference cancellation) at the receiver
  - Optimization of the radio resource: joint subcarrier and power allocation

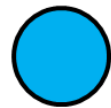
# Joint Subcarrier and Power Allocation



user 1

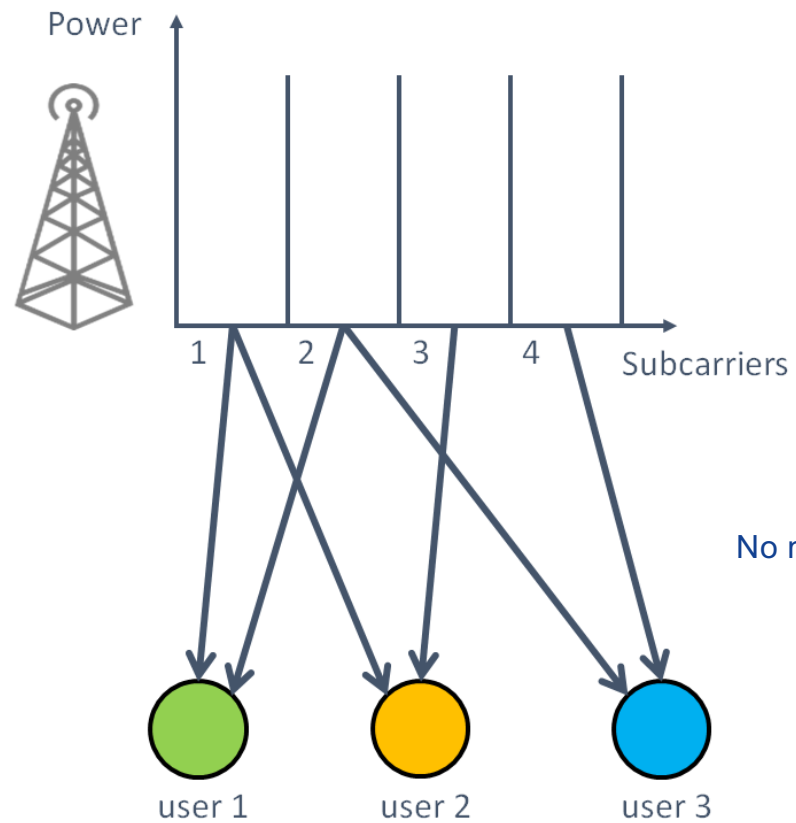


user 2



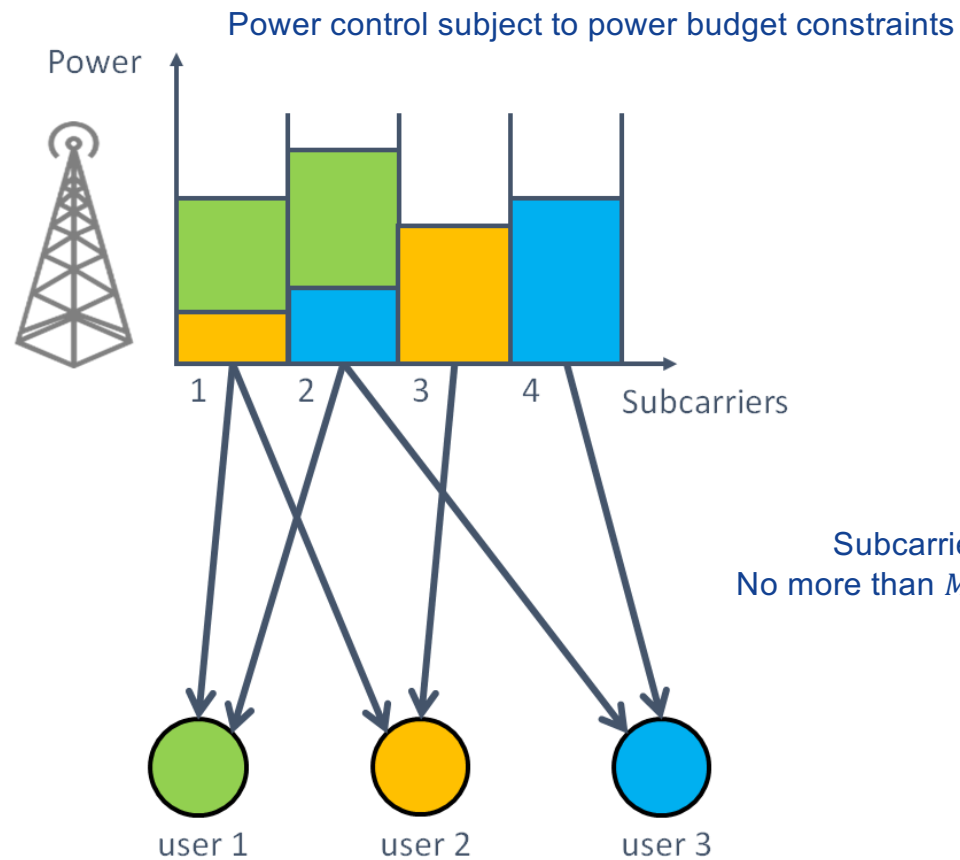
user 3

# Joint Subcarrier and Power Allocation

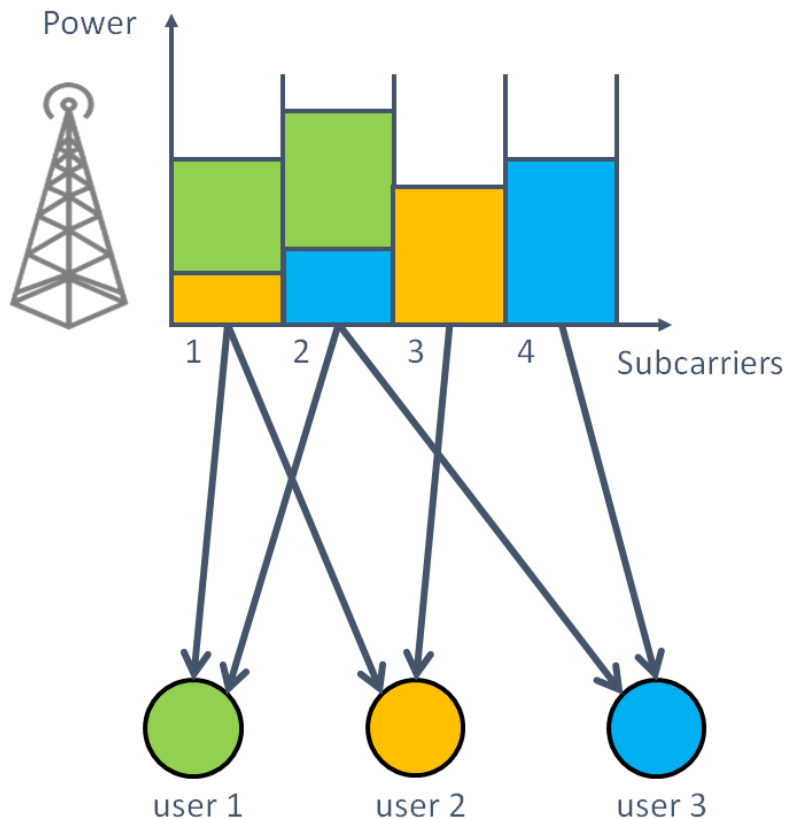


Subcarrier allocation (user selection):  
No more than  $M$  users per subcarrier (here  $M = 2$ )

# Joint Subcarrier and Power Allocation



# Joint Subcarrier and Power Allocation

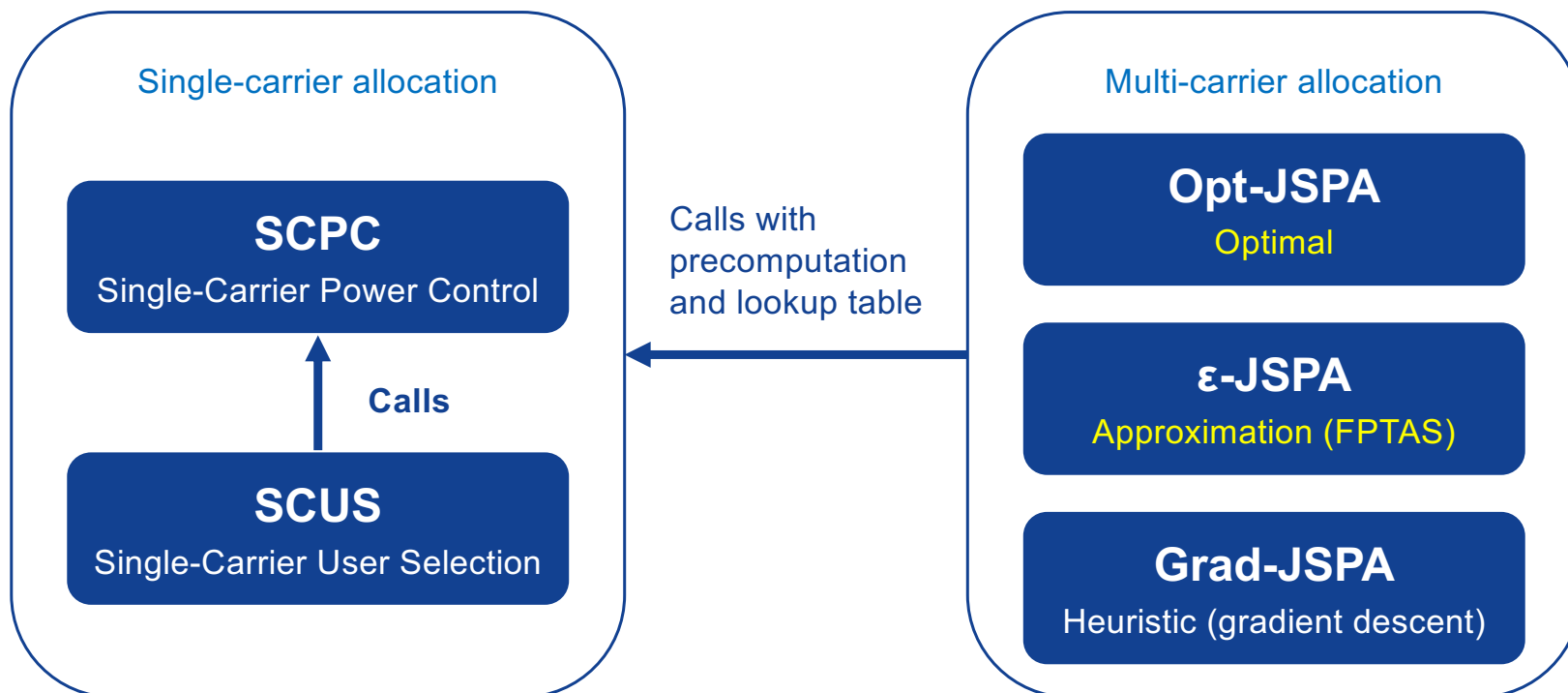


Open challenges:

- No unified framework
- No low-complexity algorithms with performance guarantees

# Radio Resource Management: an Optimization Framework

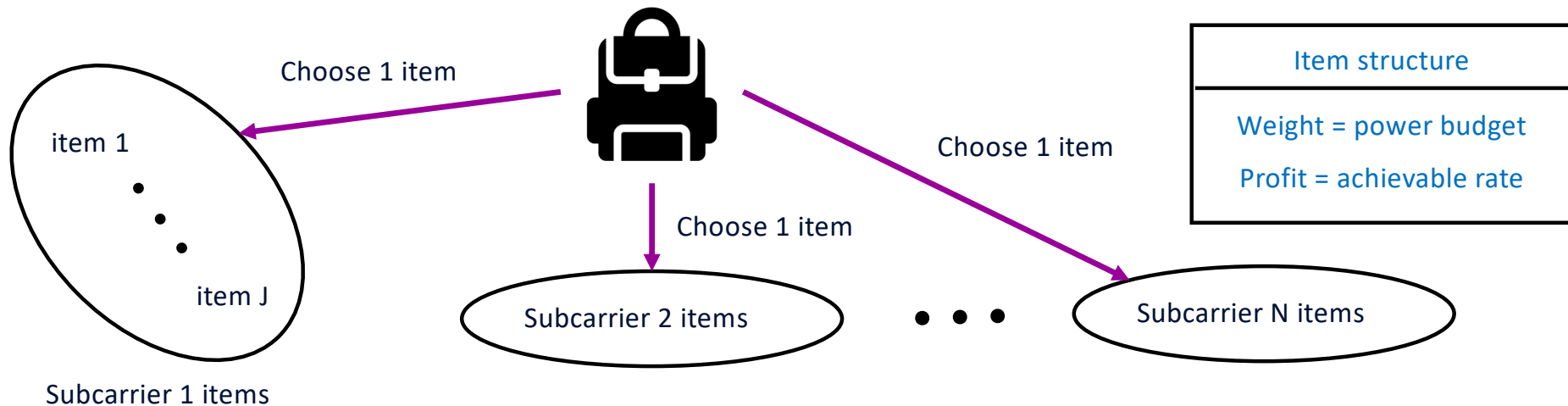
- Each module solves a sub-problem with respect to its problem structure: separability, convexity, knapsack constraints, combinatorics, etc.





# Multi-Carrier Allocation: Opt-JSPA and $\epsilon$ -JSPA

- Based on the multiple-choice knapsack problem
- Opt-JSPA: **optimal** with lower complexity than the state-of-the-art
- $\epsilon$ -JSPA: first **fully polynomial-time approximation scheme** (FPTAS) developed for this problem



# Multi-Carrier Allocation: Grad-JSPA

- Grad-JSPA: Projected Gradient Descent
- Search direction: gradient computed by **SCPC** and **SCUS** → **Separability**
- Piece-wise concave → **fast convergence to a local optimum**

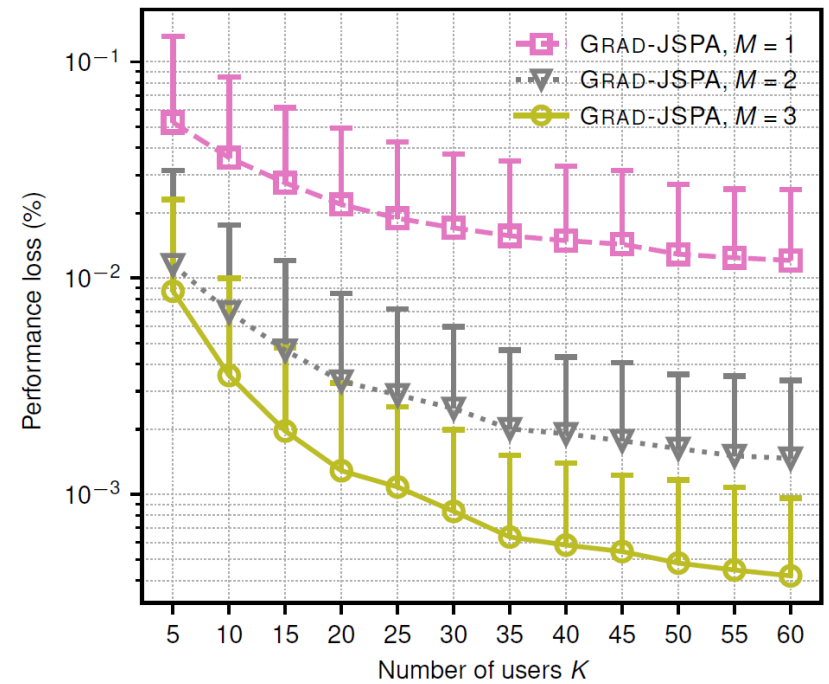
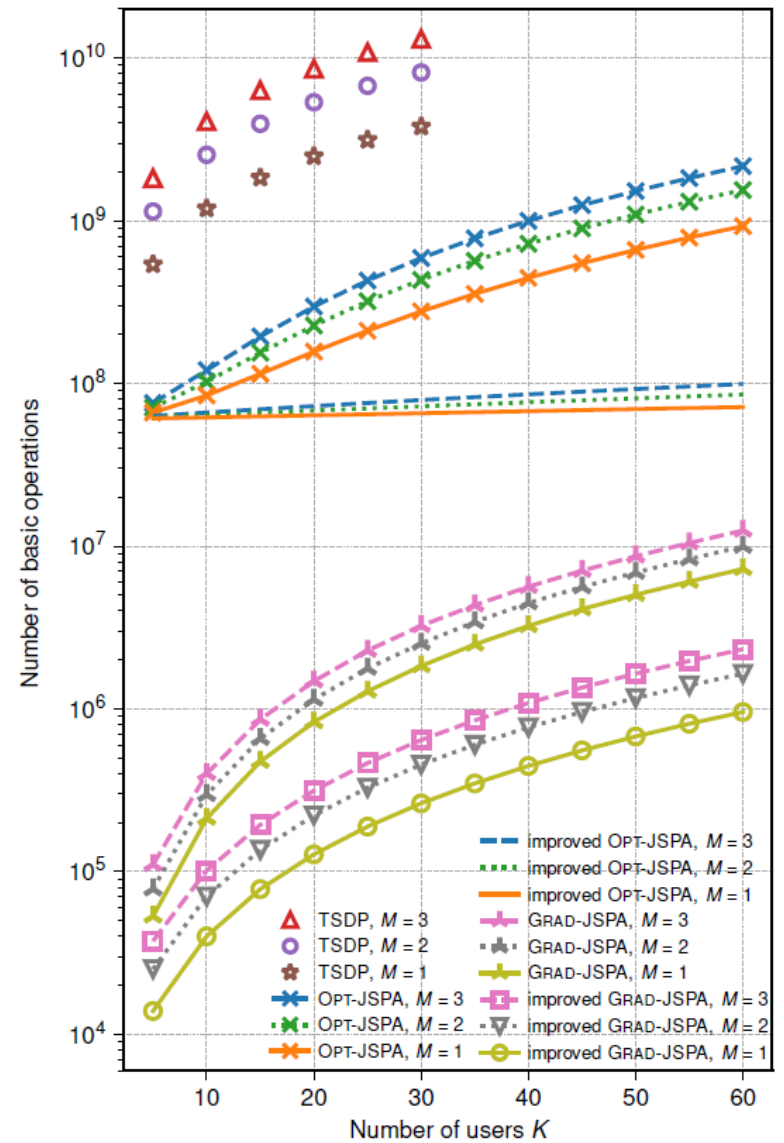


Fig. Performance loss of Grad-JSPA compared to the optimal (M: maximum number of users per subcarrier)

# Multi-Carrier Allocation:

Algorithm	Performance guarantee	Complexity for $J$ discrete power values
Monotonic optimization with outer polyblock approximation [7]	Optimal	Exponential in $K$ and $N$
TSDP [6]	Optimal	$O(J^2NMK)$
OPT-JSPA	Optimal	$O(NMK^2 + JNMK + J^2N)$
$\epsilon$ -JSPA	FPTAS	$O\left(NMK^2 + \min\left\{\log(J) \frac{N^2MK}{\epsilon} + \frac{N^3}{\epsilon^2}, JNMK + J^2N\right\}\right)$
GRAD-JSPA	Heuristic	$O(NMK^2 + \log(J)NMK)$

Decrease in complexity



# Conclusion

## Unified optimization framework for NOMA:

- Covers a general family of utility functions and system constraints:
  - Solutions under cellular power constraint (downlink): Opt-JSPA, JSPA, Grad-JSPA
  - Solutions under individual power constraints (uplink): Centralized and distributed algorithms → Nash equilibrium
- Extensive complexity and approximability analysis
- Decomposition into sub-problems with interesting properties
  - Facilitate the algorithm design
  - Provable performance guarantees
  - Extendable to new constraints and scenarios

Thank you for your attention